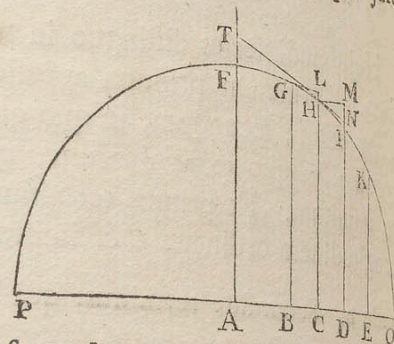


$\overline{AC}$  id est, ut tangentis longitudo illa  $HT$ , quæ ad semidiametrum  $AF$  ipsi  $PQ$  normaliter insistentem terminatur: & resistentia erit ad gravitatem ut  $3a$  ad  $2n$ , id est, ut  $3AC$  ad circuli diametrum  $PQ$ : velocitas autem erit ut  $\sqrt{CH}$ . Quare si corpus juxta ipsi  $PQ$  parallelam exeat de loco  $F$ , & medii densitas in singulis locis  $H$  sit ut longitudo tangentis  $HT$ , & resistentia etiam in loco aliquo  $H$  sit ad vim gravitatis ut  $3AC$  ad  $PQ$ , corpus illud describet circuli quadrantem  $FHQ$ . *Q. E. I.*

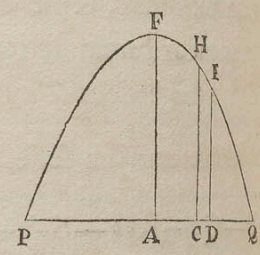


At si corpus idem de loco  $P$ , secundum lineam ipsi  $PQ$  perpendicularem egrederetur, & in arcu semicirculi  $PFQ$  moveri inciperet, sumenda esset  $AC$  seu  $a$  ad contrarias partes centri  $A$ , & propterea signum ejus mutandum esset & scribendum  $-a$  pro  $+a$ .

Quo pacto prodiret medii densitas ut  $-\frac{a}{e}$ . Negativam autem densitatem, hoc est, quæ motus corporum accelerat, natura non admittit: & propterea naturaliter fieri non potest, ut corpus ascendendo a  $P$  describat circuli quadrantem  $PF$ . Ad hunc effectum deberet corpus a medio impellente accelerari, non a resistente impediri.

*Exempl. 2.* Sit linea  $PFQ$  parabola, axem habens  $AF$  horizonti  $PQ$  perpendicularem, & requiratur medii densitas, quæ faciat ut projectile in ipsa moveatur.

Ex natura parabolæ, rectangulum  $PDQ$  æquale est rectangulo sub ordinata  $DI$  & recta aliqua data: hoc est, si dicantur recta illa  $b$ ;  $PC, a$ ;  $PQ, c$ ;  $CH, e$ ; &  $CD, o$ ; rectangulum  $a+o$  in  $c-a-o$  seu  $ac-aa-2ao+co-oo$  æquale est rectangulo



$b$  in  $DI$ , ideoque  $DI$  æquale  $\frac{ac-aa}{b} + \frac{c-2a}{b}o - \frac{oo}{b}$ . Jam scribendus esset hujus seriei secundus terminus  $\frac{c-2a}{b}o$  pro  $Qo$ , tertius

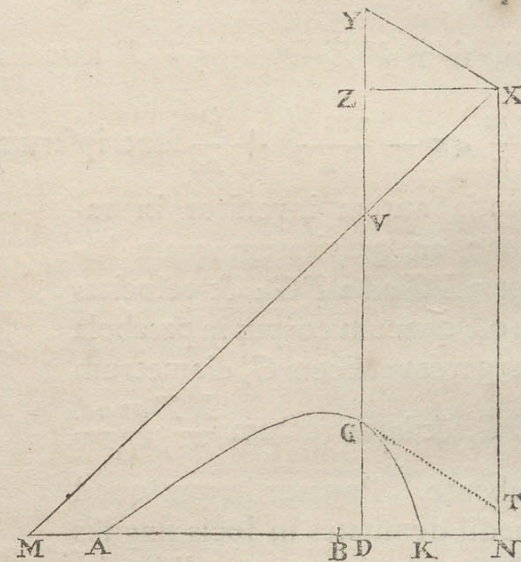
item

item terminus  $\frac{oo}{b}$  pro  $Roo$ . Cum vero plures non sint termini,  $\frac{oo}{b}$  debet quartum coefficientem  $S$  evanescere, & propterea quantitas  $\frac{S}{R\sqrt{1+QQ}}$ , cui medii densitas proportionalis est, nihil erit. Nul-

la igitur medii densitate movebitur projectile in parabola, uti olim demonstravit *Galilæus. Q. E. I.*

*Exempl. 3.* Sit linea  $AGK$  hyperbola, asymptoton habens  $NX$  plano horizontali  $AK$  perpendicularem; & quærat medii densitas, quæ faciat ut projectile moveatur in hac linea.

Sit  $MX$  asymptotos altera, ordinatim applicatæ  $DG$  productæ occurrens in  $V$ ; & ex natura hyperbolæ, rectangulum  $XV$  in  $VG$  dabitur. Datur autem ratio  $DN$  ad  $VX$ , & propterea datur etiam rectangulum  $DN$  in  $VG$ . Sit illud  $bb$ : & completo parallelogrammo  $DNXX$ ; dicatur  $BN, a$ ;  $BD, o$ ;  $NX, c$ ; & ratio data  $VZ$  ad  $ZX$  vel  $DN$  ponatur esse  $\frac{m}{n}$ . Et erit  $DN$  æqualis  $a-o$ ,  $VG$  æqualis



$\frac{bb}{a-o}$ ,  $VZ$  æqualis  $\frac{m}{n} \frac{a-o}{a}$ , &  $GD$  seu  $NX - VZ - VG$  æqualis  $c - \frac{m}{n}a + \frac{m}{n}o - \frac{bb}{a-o}$ . Resolvatur terminus  $\frac{bb}{a-o}$  in seriem convergentem  $\frac{bb}{a} + \frac{bb}{aa}o + \frac{bb}{a^2}oo + \frac{bb}{a^3}o^3$  &c. & fiet  $GD$  æqualis  $c - \frac{m}{n}a - \frac{bb}{a} + \frac{m}{n}o - \frac{bb}{aa}o - \frac{bb}{a^2}o^2 - \frac{bb}{a^3}o^3$  &c. Hujus seriei terminus secundus  $\frac{m}{n}o - \frac{bb}{aa}o$  usurpandus est pro  $Qo$ , tertius cum signo mutato  $\frac{bb}{a^2}o^2$  pro  $Ro^2$ , & quartus cum signo etiam mutato  $\frac{bb}{a^3}o^3$  pro

L 1